

Application nr. 7 (Connections)

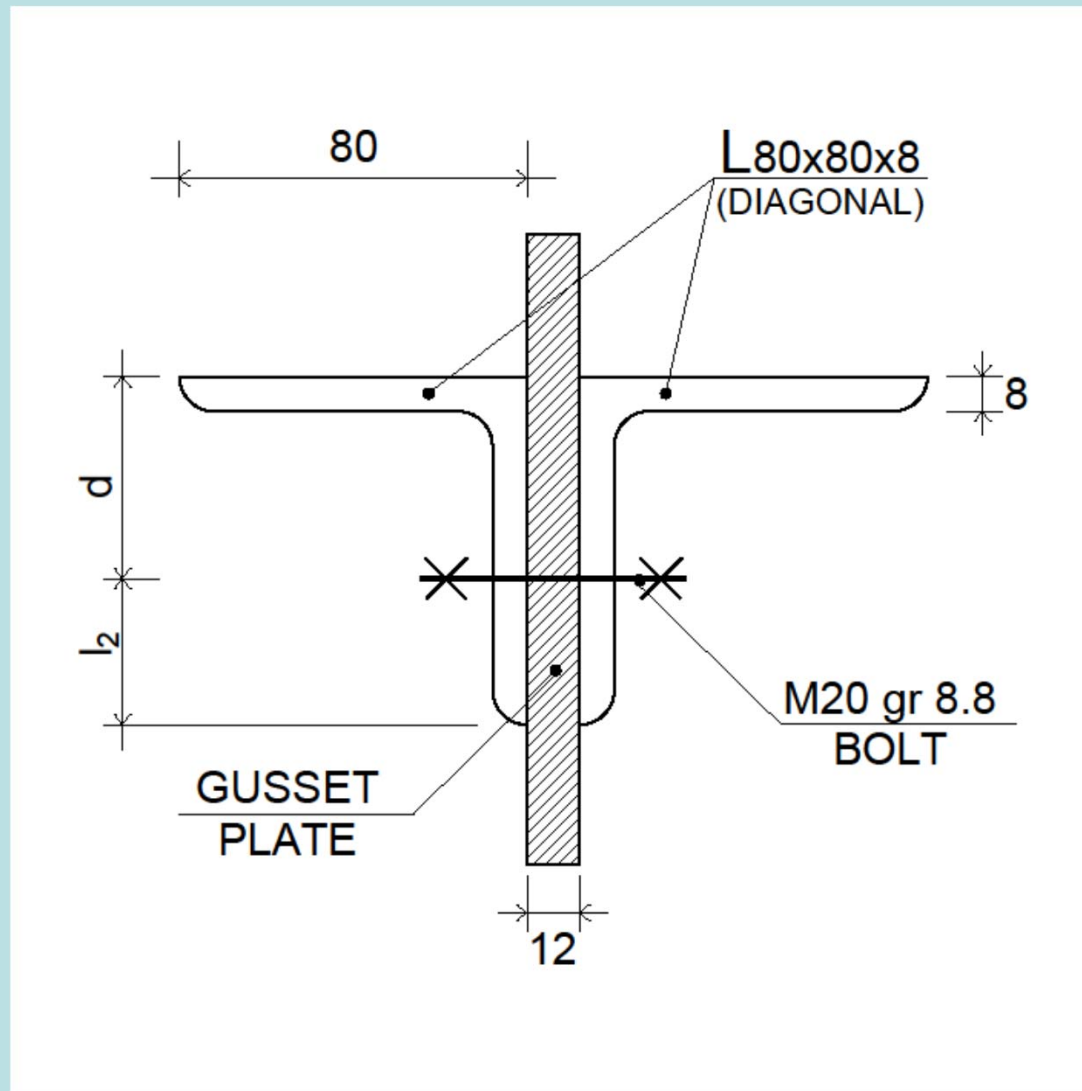
Strength of bolted connections
to EN 1993-1-8 (Eurocode 3, Part 1.8)

PART 1:
Bolted shear connection
(Category A – bearing type, to
EN1993-1-8)

Structural element

- Tension diagonal made of two angle sections, with bolted end connection on gusset plate;
- This is a shear type connection category A to EN 1993-1-8 (shear connection of bearing type)

Diagonal cross-section with bolted connection:



Initial data:

- Axial load acting on diagonal: $N=+46.000$
daN = 460 kN
- Steel grade for angle section and gusset plate: S235
- Angle section type: L 80x80x8
- Required bolts: M20 gr.10.9
- Gusset plate thickness: $t=12$ mm
- Bolt nominal diameter $d=20$ mm = 2,0 cm

Resulting data:

- For the steel in the angle section and gusset plate:

$$f_y = 2350 \text{ daN/cm}^2 = 235 \text{ N/mm}^2$$

$$f_u = 3700 \text{ daN/cm}^2 = 370 \text{ N/mm}^2$$

Grade indicators

- For the steel in the M20 gr.10.9 bolts:

$$f_{yb} = 10 \times 9 = 90 \text{ daN/mm}^2 = 900 \text{ N/mm}^2$$

$$f_{ub} = (10) \times 10 = 100 \text{ daN/mm}^2 = 1000 \text{ N/mm}^2$$

Grade indicator

a) Sizing of the bolt group

- This is a shear connection of bearing type
- The sizing should refer to:
 - The shear resistance of the bolt
 - The bearing resistance of the bolt

Shear resistance of the bolt

- Two shear planes exist in the end connection of the member
- The shear resistance of the bolt per shear plane is (non-threaded shank in shear):

$$F_{v,Rd} = \frac{\alpha_v \cdot f_{ub} \cdot A}{\gamma_{M2}}$$

$$A = \frac{\pi \cdot d^2}{4} = \frac{\pi \cdot 2^2}{4} = 3,14 \text{ cm}^2$$

- $\alpha_v = 0,5$ (for grade 10.9 bolts)
- $\gamma_{M2} = 1,25$

Shear resistance of the bolt:

- The shear resistance of the bolt for the two shear planes results:

$$2 \cdot F_{v,Rd} = 2 \cdot \frac{0,5 \cdot 100000 \cdot 3,14}{1,25} = 25.120 \text{ daN}$$

Bearing resistance of the bolt:

- The **minimum thickness package** in this case is the gusset plate, having a plate thickness of $t=12$ mm;
- This thickness is less than the sum of angle leg thickness:

$$2 \times t_1 = 2 \times 8,0 \text{ mm} = 16,0 \text{ mm} > t$$

The bearing resistance:

$$\left\{ \begin{array}{l} F_{b,Rd} = \frac{k_1 \cdot f_u \cdot \alpha_b \cdot d \cdot t}{\gamma_{M2}} \\ \alpha_b = \min \left\{ \frac{f_{ub}}{f_u}; 1,0; \alpha_d \right\} \end{array} \right.$$

In our application:

$$\frac{f_{ub}}{f_u} = \frac{10000}{3700} = 2,70 > 1,0$$

M20 gr.10.9 bolts are usually installed in clearance holes:

- A usual hole clearance would be of 2 mm for M20 bolts (diameter less than 24 mm)
- Consequently, the hole diameter (d_0) results:

$$d_0 = 22 \text{ mm} > d = 20 \text{ mm}$$

Calculation of the α_d value

The **end distance** of the bolt (i.e. distance between the last bolt of the group and end of the diagonal profile)

$$e_1 = 1,5 \times d_0 = 33,0 \text{ mm} > e_{1.\text{min}} = 1,2d_0$$

$$\left\{ \begin{array}{l} \alpha_d = \frac{e_1}{3 \cdot d_0} = \frac{33}{3 \cdot 22} = 0,5 \\ \Rightarrow \alpha_b = 0,5 \end{array} \right.$$

Coefficient k_1 in the bearing resistance $F_{b,Rd}$ formula:

- The coefficient k_1 is the minimum between following values:

$$\left\{ \begin{array}{l} k_1 = \min \left\{ 2,8 \cdot \frac{e_2}{d_0} - 1,7 ; 2,5 \right\} \\ 2,8 \cdot \frac{e_2}{d_0} - 1,7 = 2,8 \cdot \frac{1,5 \cdot d_0}{d_0} - 1,7 = 2,5 \\ \Rightarrow k_1 = 2,5 \end{array} \right.$$

The bearing resistance of the gusset plate for M20 bolt results:

$$F_{b,Rd} = \frac{2,5 \cdot 3700 \cdot 0,5 \cdot 2,0 \cdot 1,2}{1,25} = 8880 \text{ daN}$$

Sizing of the bolt group:

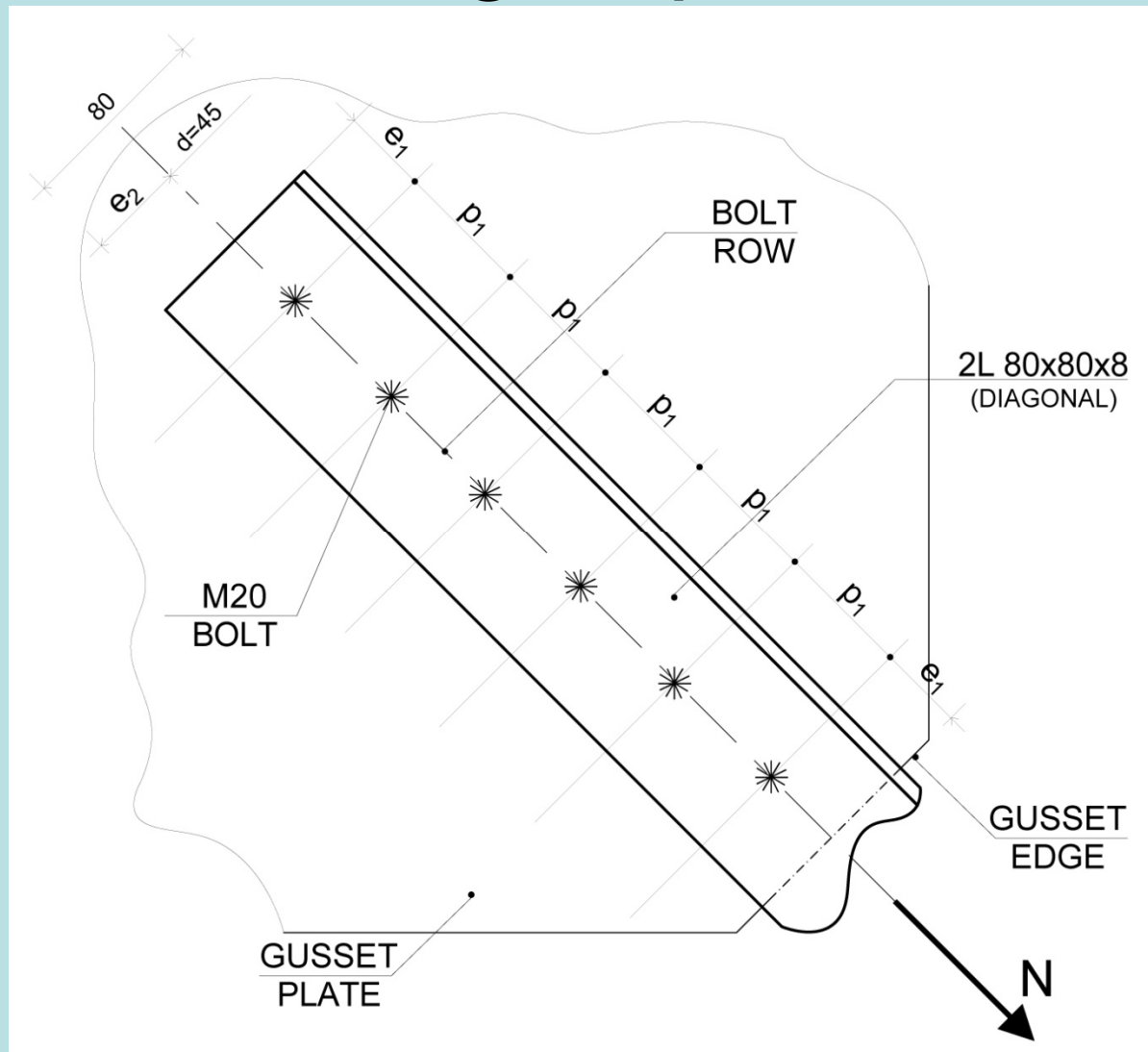
- The capacity of one bolt in the group (F_1) is the minimum between shear and bearing resistance:

$$F_1 = \min \{ 2 \cdot F_{v,Rd} ; F_{b,Rd} \} = 8880 \text{ daN}$$

- The **necessary number of bolts** results as (supposing an equal distribution of the shear force):

$$n_b = \frac{N}{F_1} = \frac{46000}{8880} = 5,18 \cong 6,0 \text{ bolts}$$

b) Bolt arrangement and checking of the bolt group resistance



In the previous drawing showing the bolted connection final geometry:

e_1 = distance between the **first / last bolt of the group and gusset edge / angle end** (measured parallel to axial force direction)

e_2 = distance between **bolts and edge** measured perpendicular to axial force direction

p_1 = distance between **consecutive bolts** measured parallel to axial force direction

In the first phase we know only the number of bolts (i.e. 6 bolts):

- Distances e_1, e_2, p_1 are **initially unknown** and have to be chosen by the designer according to the recommendations of Table 3.3 from EN1993-1-8
- For e_1, e_2 , and p_1 we generally choose rounded values (i.e. multiple of 5 mm):

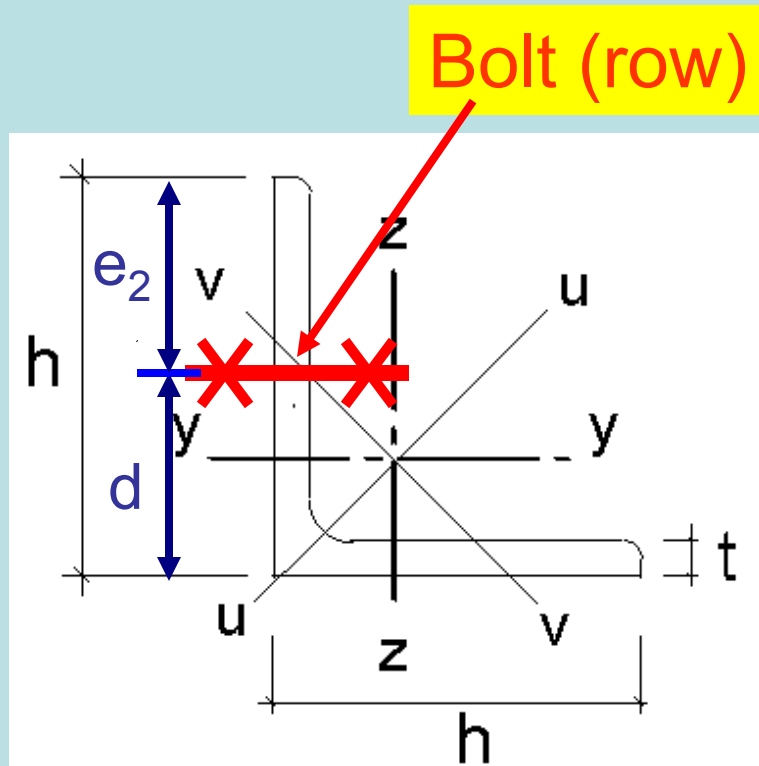
$$e_1 = 35 \text{ mm} = 1,59d_0 > 1,2d_0$$

$$e_2 = 35 \text{ mm} = 1,59d_0 > 1,2d_0$$

$$p_1 = 55 \text{ mm} = 2,50d_0 > 2,2d_0$$

- As a principle $e_1, e_2,$ and p_1 should be chosen closer to the minimum recommended values in order to get a connection as small as possible;
- The 6 bolts resulting from the previous calculation are disposed on a single bolt row;
- The number of bolts in the row is six, i.e. the maximum permitted number in a row allowing for an **equal distribution of the shear force on the connection.**

Observation regarding e_2 distance:



In an angle section with the length of the leg = h , the recommended position of the bolt row (measured from the corner) is:

$$d = h/2 + 5 \text{ mm}$$

In our case, $d = 80/2 + 5 = 45 \text{ mm}$

That solves also the problem for the bolt-to-edge distance, measured on perpendicular direction to the axial force N (e_2) i.e.:

$$e_2 = h - d = 80 - 45 = 35 \text{ mm}$$

$$\text{Thus } e_2 = 1,59d_0 > 1,2d_0$$

Checking of the bolt group (using actual connection geometry):

- Shear resistance per bolt:

$$2 \cdot F_{v,Rd} = 25.120 daN$$

- Bearing resistance per bolt:

$$F_{b,Rd} = \frac{k_1 \cdot \alpha_b \cdot f_u \cdot d \cdot t}{\gamma_{M2}}$$

$$\begin{cases} k_1 = 2,8 \cdot \frac{e_2}{d_0} - 1,7 = 2,8 \cdot \frac{35}{22} - 1,7 = 2,75 > 2,5 \\ \Rightarrow k_1 = 2,5 \end{cases}$$

Calculation of the (α_b) value:

$$\begin{cases} \alpha_d = \frac{e_1}{3 \cdot d_0} = \frac{35}{3 \cdot 22} = 0,53 \\ \frac{f_{ub}}{f_u} = \frac{10000}{3700} = 2,70 \\ \Rightarrow \alpha_b = \min \left\{ \alpha_d; \frac{f_{ub}}{f_u}; 1,0 \right\} = 0,53 \end{cases}$$

- Bearing resistance of the gusset plate:

$$F_{b,Rd} = \frac{2,5 \cdot 0,53 \cdot 3700 \cdot 2,0 \cdot 1,2}{1,25} = 9413 \text{ daN}$$

- Bolt resistance is:

$$\min \{ 2F_{v,Rd}; F_{b,Rd} \} = \min \{ 25120; 9413 \} = 9413 \text{ daN}$$

- The design shear force acting on the bolt is obtained admitting an **equal (even) distribution of the axial force N on all bolts**;
- This is acceptable because the code recommendation to provide a maximum number of 6 bolts per row has been **respected** in our example;
- Equivalently, between the first and the last bolt of the row we have the distance = $5 \times 55 \text{ mm} = 275 \text{ mm} < 15 \cdot d = 15 \times 20 \text{ mm} = 300 \text{ mm}$

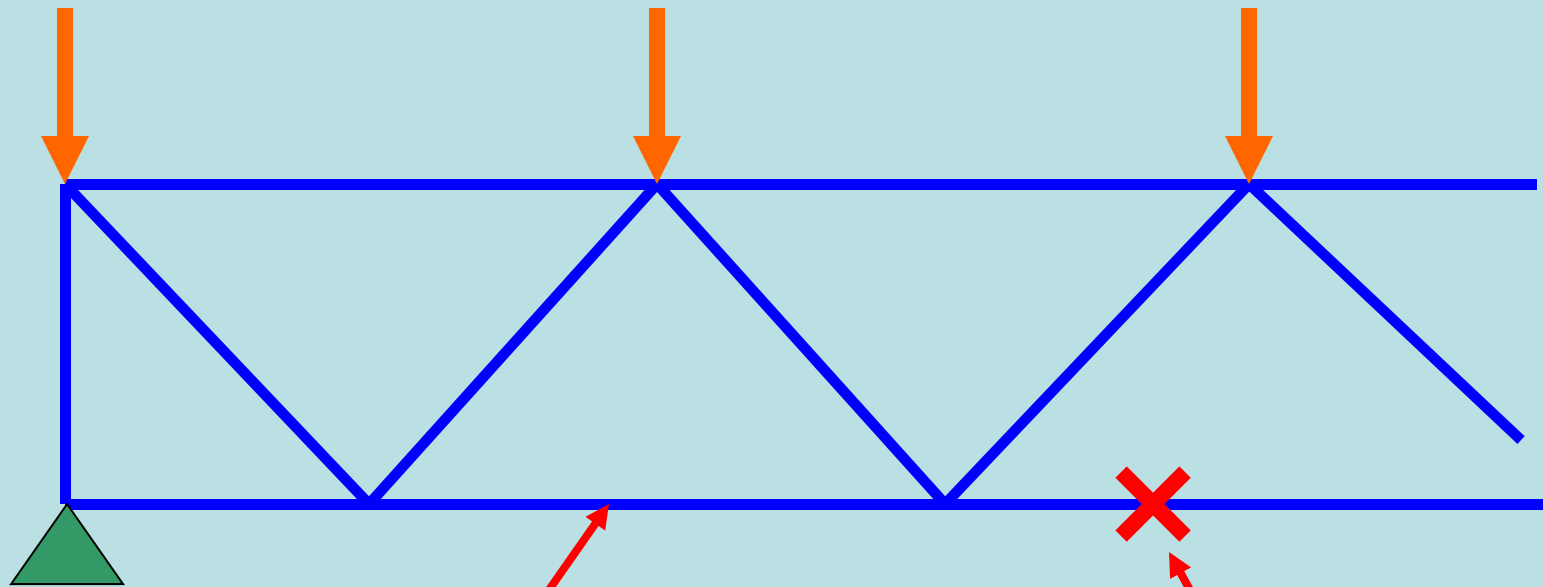
$$F_{v,Ed} = \frac{N}{6} = \frac{46000}{6} = 7.666 \text{ daN} < 9413 \text{ daN} = F_{b,Rd}$$

- Checking according to Code Table 3.2 is OK !

PART 2:

Bolted connection in tension only
(end-plate splice) –Category D –
non-preloaded to EN 1993-1-8

Position of the end plate splice (connection) in a lattice girder



Bottom chord in tension

End plate connection

Initial data:

- Bottom chord in tension of a lattice girder
- Bottom chord profile: circular hollow section: CHS- Φ 121x8 mm
- Steel grade: S235
- Axial force $N=+50.000$ daN = 500 kN
- Required connection: end-plate splice
- Required bolts: M16 gr.8.8
- End plate thickness $t=16$ mm
- Bolt nominal diameter $d=16$ mm = 1,6 cm

Observation on the end plate thickness value ($t=16$ mm):

- As an **empirical rule of good practice**, for any end plate it is recommended to choose a thickness value **greater-equal to the diameter of the employed bolts** in the connection;
- Thus, here $t = d = 16$ mm !
- This is generally avoiding the prying effect in the connection (excessive deformability of the end plate)

Resulting data:

- For the required steel grade:

$$f_y = 235 \text{ N/mm}^2$$

$$f_u = 370 \text{ N/mm}^2$$

- For the required bolt grade:

$$f_{yb} = 8 \times 8 = 64 \text{ daN/mm}^2 = 640 \text{ N/mm}^2$$

$$f_{ub} = 8 \times 10 = 80 \text{ daN/mm}^2 = 800 \text{ N/mm}^2$$

Resistant area of the M16 bolt:

- For the required M16 gr.8.8 bolts, the nominal diameter is $d=16 \text{ mm} = 1,6 \text{ cm}$
- The resistant diameter of the bolt is evaluated with: $d_{res} = 0,89 \cdot d = 0,89 \cdot 1,6 = 1,424 \text{ cm}$
- The resistant area results:

$$A_s = A_{res} = \frac{\pi \cdot d_{res}^2}{4} = \frac{\pi \cdot 1,424^2}{4} = 1,592 \text{ cm}^2$$

Tension resistance of M16 gr.8.8 bolt according to Table 3.4:

- The tension resistance of the bolt results from the formula:

$$F_{t,Rd} = \frac{k_2 \cdot f_{ub} \cdot A_s}{\gamma_{M2}} = \frac{0,9 \cdot 8000 \cdot 1,592}{1,25} = 9170 \text{ daN}$$

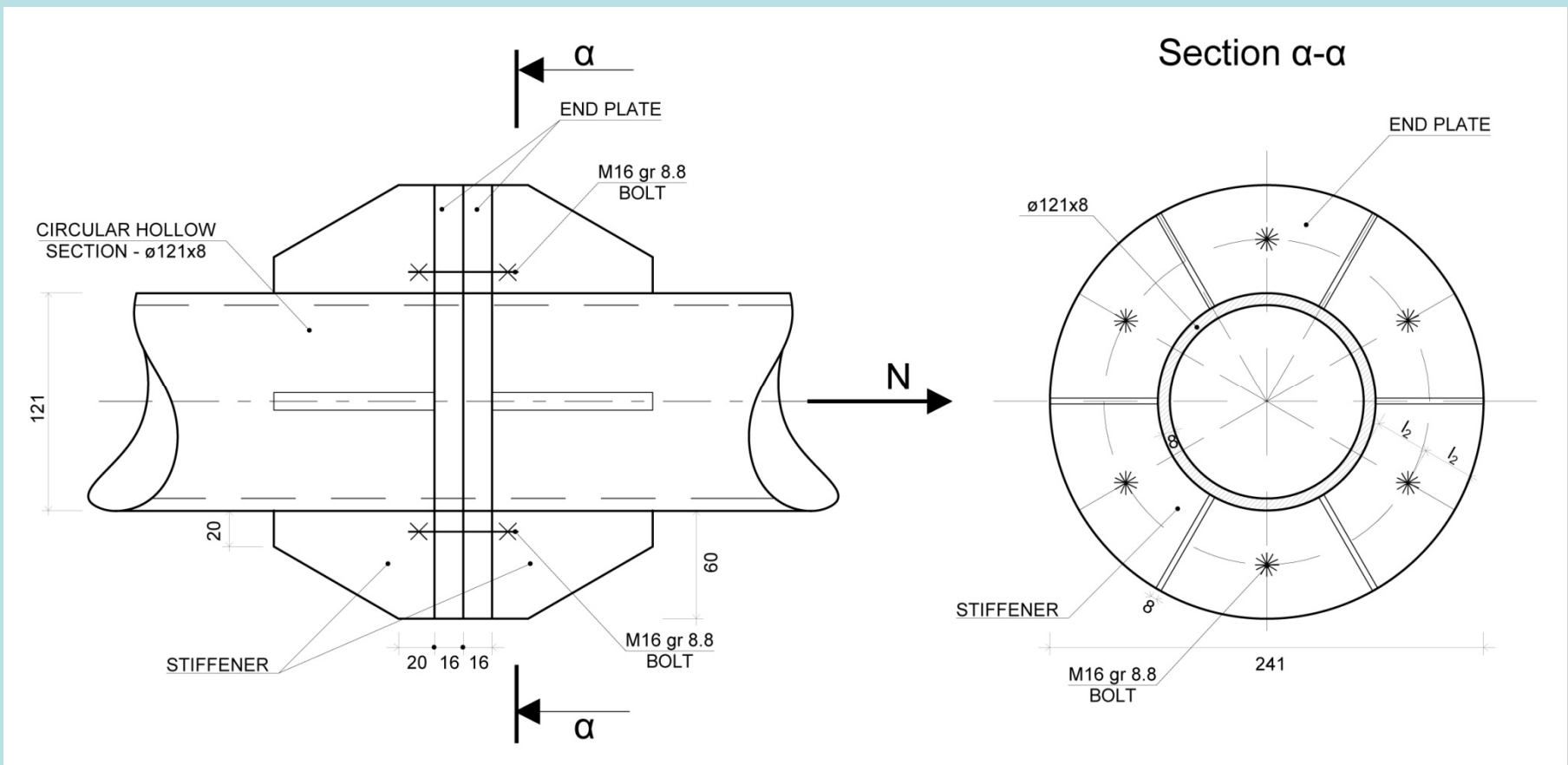
- Where A_s = tensile stress area of the bolt = A_{res}
- $K_2 = 0,9$ (to the code for regular bolts)

Sizing of the end-plate connection with bolts in tension only:

- The axial force N is equally distributed on all the bolts of the connection;
- The **required number of bolts** is unknown in this phase;
- The required number of M16 bolts results from the sizing procedure, i.e.:

$$n_{bolt} = \frac{N}{F_{t,Rd}} = \frac{50000}{9170} = 5,45 \cong 6 \text{ bolts}$$

Resulting geometry of the end-plate connection in tension:



Comment on the connection geometry (1):

- The M16 bolts are installed in clearance holes with a diameter $d_0 = 16\text{mm} + 2\text{mm} = 18\text{ mm}$
- The distances between bolt centre and the pipe wall respectively end plate edge have been taken according to Table 3.3:

$$e_1 = e_2 = 30\text{ mm} = 1,67 \cdot d_0 > 1,2d_0$$

Comment on the connection geometry (2):

- The **provision of the stiffeners**, connecting the end plate to the pipe and separating the bolts has two purposes:
 - A stronger connection between pipe and the end plate
 - Reduction of the end-plate deformability in order to **eliminate prying effect** (bending of the bolt shank owing to end-plate deformability)

Checking of the end-plate connection:

- The analyzed connection is a tension connection of **category D (non-preloaded)** according to Table 3.2
- The checking formulae to Table 3.2 are:

$$\begin{cases} F_{t,Ed} \leq F_{t,Rd} \\ F_{t,Ed} \leq B_{p,Rd} \end{cases}$$

Meaning of the terms in checking formulae:

- $F_{t,Ed}$ = design tensile force per bolt, obtained from loading;
- $F_{t,Rd}$ = tension resistance per bolt according to Table 3.4;
- $B_{p,Rd}$ = punching shear resistance (of the end plate) according to Table 3.4

Calculation of the design tensile force per bolt:

- All the six bolts are equally loaded from the tensile force $N=500$ kN applied on the connection (on the splice)
- The design tensile force per bolt results:

$$F_{t,Ed} = \frac{N}{6} = \frac{500000}{6} = 83333 \text{ daN}$$

- Observation: An equal distribution of the tensile force N on the bolts is assumed!

Calculation of the tension resistance of the bolt to Table 3.4:

- Previously performed, i.e.:

$$F_{t,Rd} = \frac{k_2 \cdot f_{ub} \cdot A_s}{\gamma_{M2}} = \frac{0,9 \cdot 8000 \cdot 1,592}{1,25} = 9170 \text{ daN} > F_{t,Ed} = 8333 \text{ daN}$$

- First condition of Table 3.4 is thus checked!

Calculation of the punching shear resistance of the end-plate

- The **punching shear resistance** according to Table 3.4 is referring to the **end plate failure by punching under the bolt head**;
- The formula is:

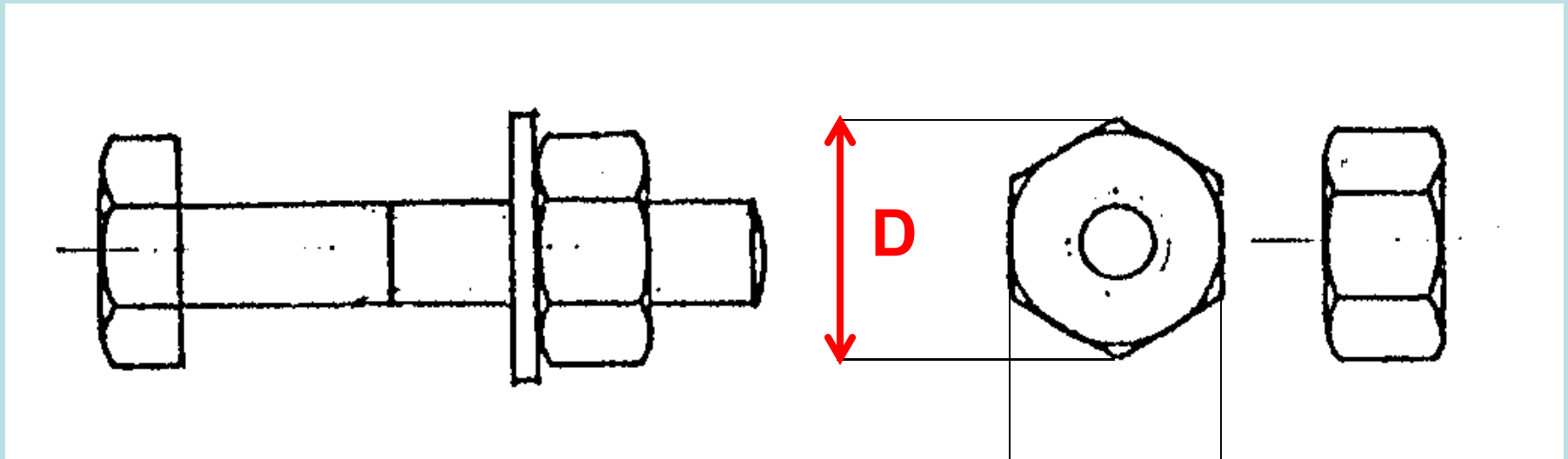
$$B_{p,Rd} = \frac{0,6 \cdot \pi \cdot d_m \cdot t_p \cdot f_u}{\gamma_{M2}}$$

- where f_u = ultimate stress of the end plate steel

Explanation of the terms in the punching resistance formula:

- d_m = the mean of the **across-points** (D) and **across-flats** (S) dimensions of the bolt head or of the nut (whichever is smaller)
- These dimensions (i.e. **D** and **S**) are usually found in the tables containing the geometric characteristics for bolts (in this case high strength bolts)
- In common practice the values are identical between bolt head and nut.

Geometry of the bolt head (nut)



Values of D and S dimensions [mm] for different types of high strength bolts:

Bolt type	M12	M16	M20	M22	M24	M27
D	24,9	30,5	36,2	40,7	46,3	52,0
S	22	27	32	36	41	46

Calculation of the d_m value:

- For the M16 gr.8.8 bolt head and nut, we get:

$$d_m = \frac{D + S}{2} = \frac{30,5 + 27}{2} = 28,75 \text{ mm}$$

- The value is identical either for the bolt head or for the nut.

Calculation of the punching resistance $B_{p,Rd}$ of the end plate:

- Using the **end plate thickness** $t=16$ mm, we are able now to calculate the punching resistance of the end plate under the bolt head (or nut):

$$B_{p,Rd} = \frac{0,6 \cdot \pi \cdot 2,875 \cdot 1,6 \cdot 3700}{1,25} = 25.652 \text{ daN} > F_{t,Ed} = 8333 \text{ daN}$$

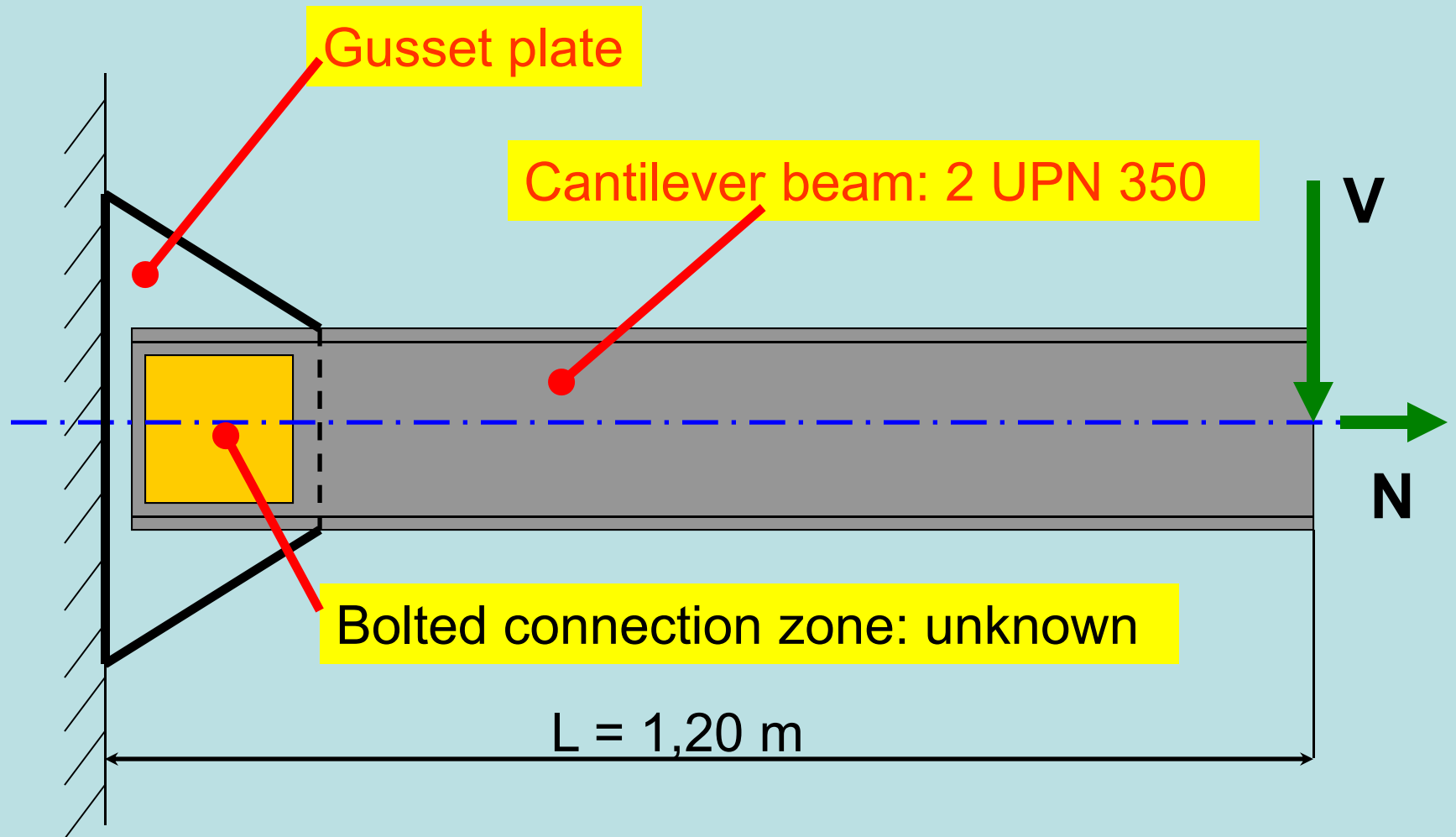
- The second condition of Table 3.4 is thus checked! This concludes the checking procedure.

PART 3:

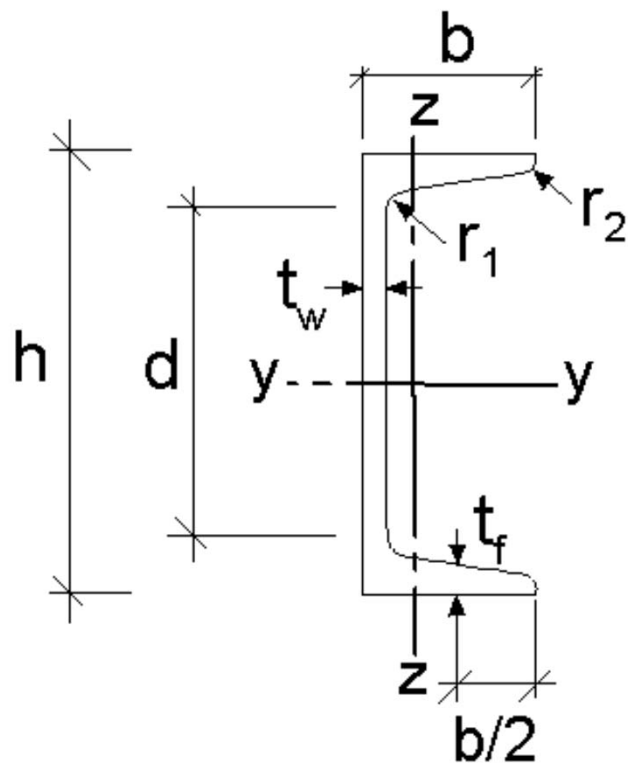
Shear connection under shear force
and bending moment. Version 1:

Category A shear connection of
bearing type

Static scheme of the connection:



A cantilever beam is required, made of two UPN 350 channel sections



Geometrical characteristics of the profile:

$$h = 350 \text{ mm}$$

$$b = 100 \text{ mm}$$

$$t_w = 14 \text{ mm}$$

$$t_f = 16 \text{ mm}$$

The problem requires the design of the cantilever beam support as a **bolted connection of Category A – bearing type**

- INITIAL DATA:
- $V = 80 \text{ kN} = 8.000 \text{ daN}$ (shear load)
- $N = 60 \text{ kN} = 6.000 \text{ daN}$ (axial load)
- Cantilever span: $L=1,20 \text{ m}$
- Steel grade: S275
- Gusset thickness $t_g = 15 \text{ mm}$
- Grade of the bolts = gr.5.6 (bolt diameter **unknown in the initial phase**)

First step: finding out the recommended diameter of the bolt

- The recommended diameter of the bolt may be found using the following **empiric relation**:

$$d = \sqrt{5 \cdot t_{\min} [cm]} - 0,4$$

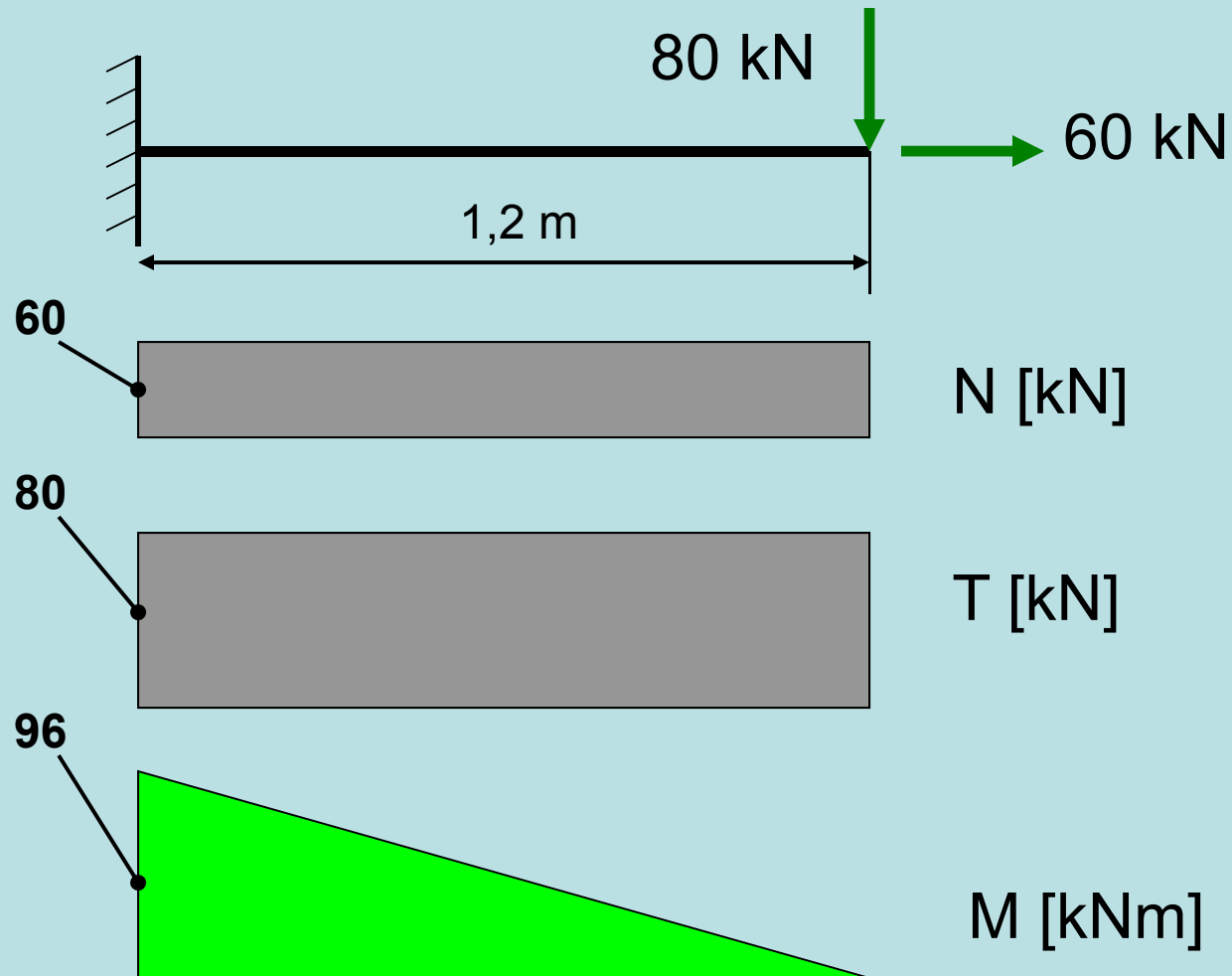
- Where $t_{\min} [cm]$ = minimum thicknes between the connected plates, in centimeters (in our case the UPN 350 web thickness = 14 mm = 1,4 cm);

- Applying the empiric formula in our particular case gives:

$$d[cm] = \sqrt{5 \cdot 1,4} - 0,4 = 2,25 \text{ cm} \cong 22 \text{ mm}$$

- By practical reason (availability on the market) **an M20 bolt is chosen for further calculation.**
- Upper relation correlates the **diameter of the employed bolts** with the **thickness of the plates** in the connected package.
- This is always necessary in order to avoid bearing failure of the plates.

Internal efforts from loading on the cantilever beam:



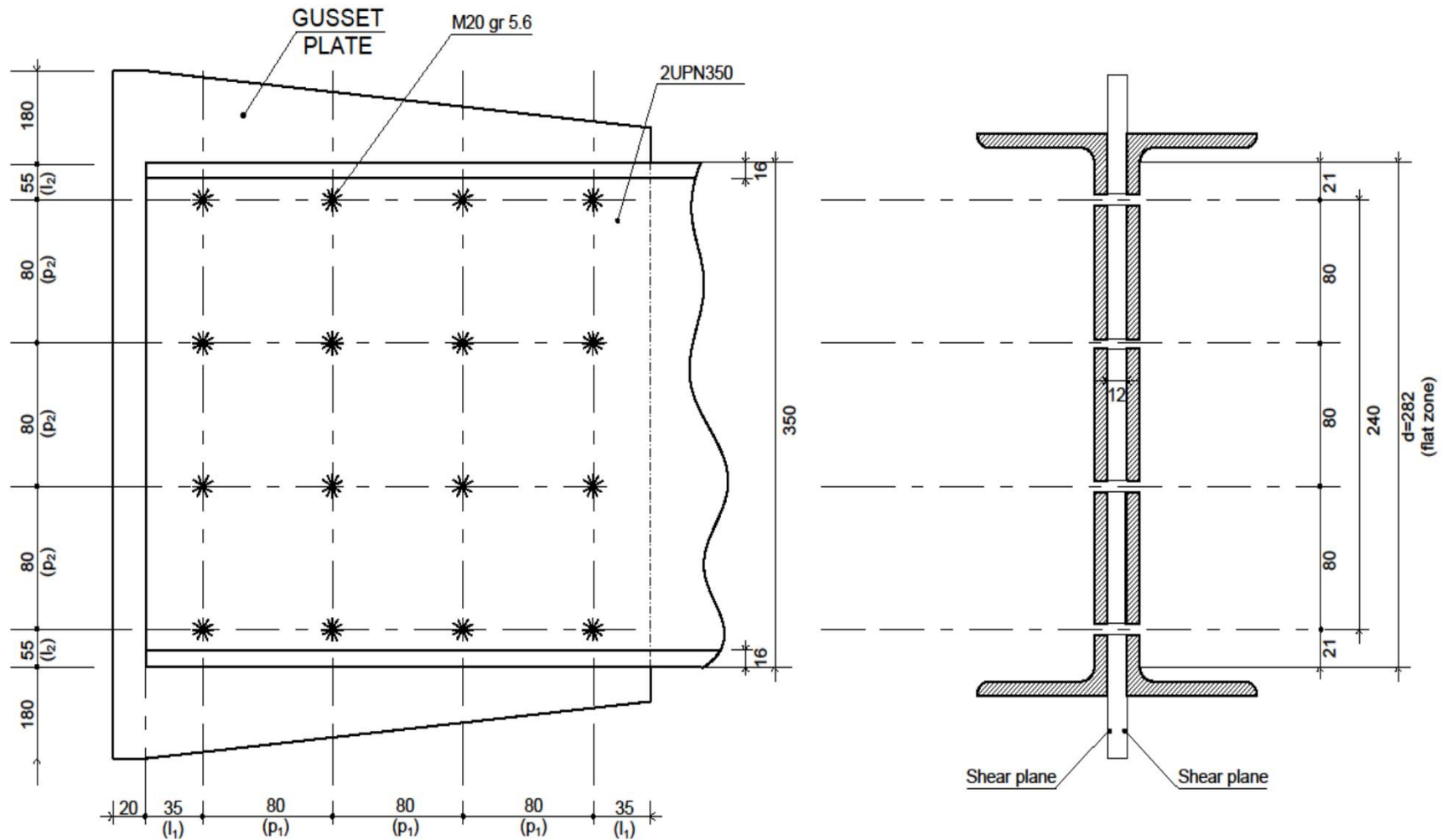
Observation and start of design:

- In the support zone of the cantilever beam, as visible from the previous diagrams, a complex state internal efforts exists, i.e.:
 - Axial force $N = 60 \text{ kN}$
 - Shear force $T = 80 \text{ kN}$
 - Bending moment $M = 96 \text{ kNm}$
- Because of this **complex state of internal efforts**, a simple sizing calculation (as in the previous examples) to establish the number of bolts for the connection **is NOT possible!**

Start of the design procedure:

- To start the design procedure, the designer shall propose a number of bolts and a geometry for the connection, according to his experience.
- The proposed connection will be then checked according to the conditions for category A connection (bearing type) required in the problem.
- After calculation and conclusions, corrections will be performed on initial bolt group if necessary.

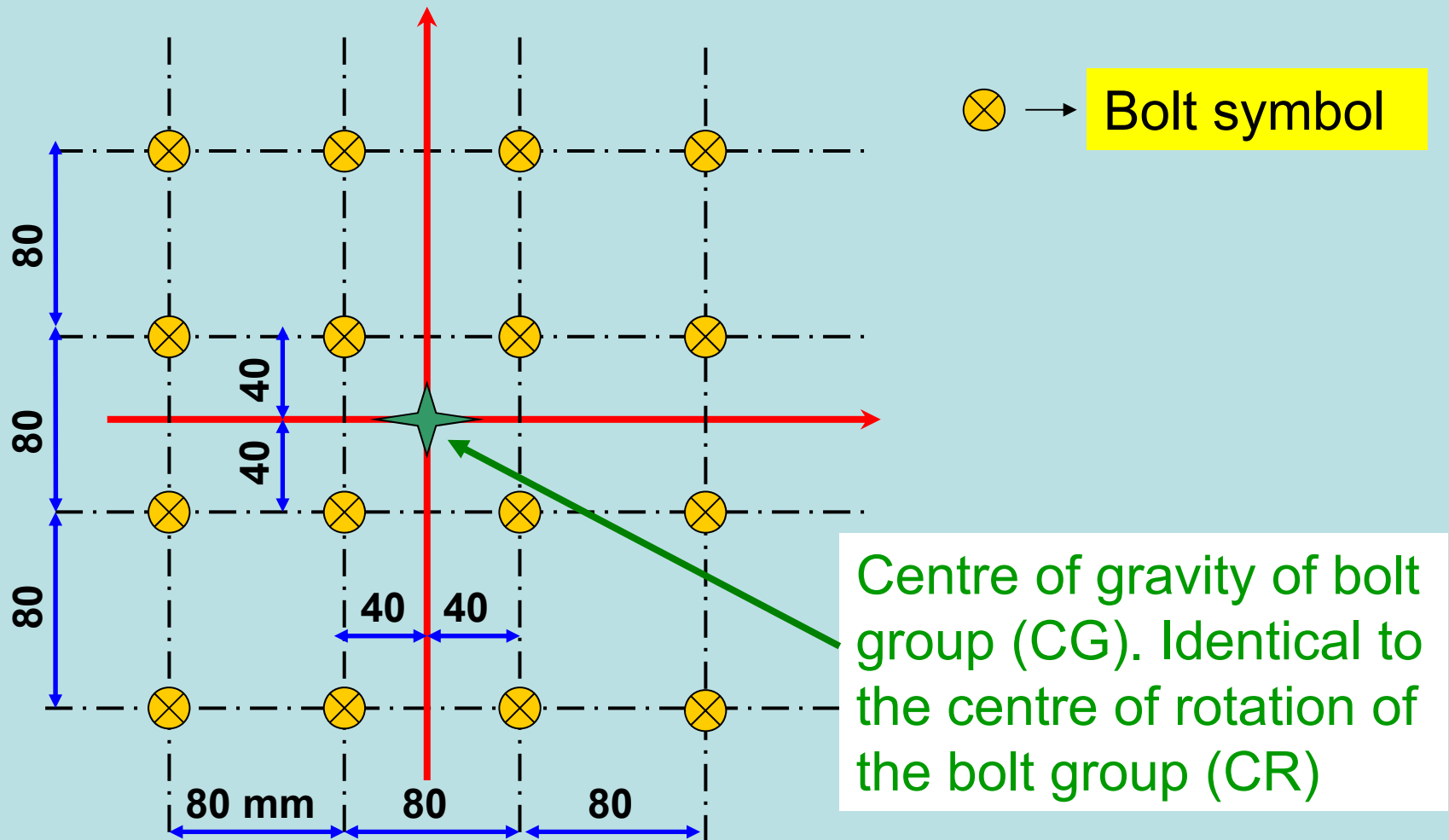
Proposed bolted connection



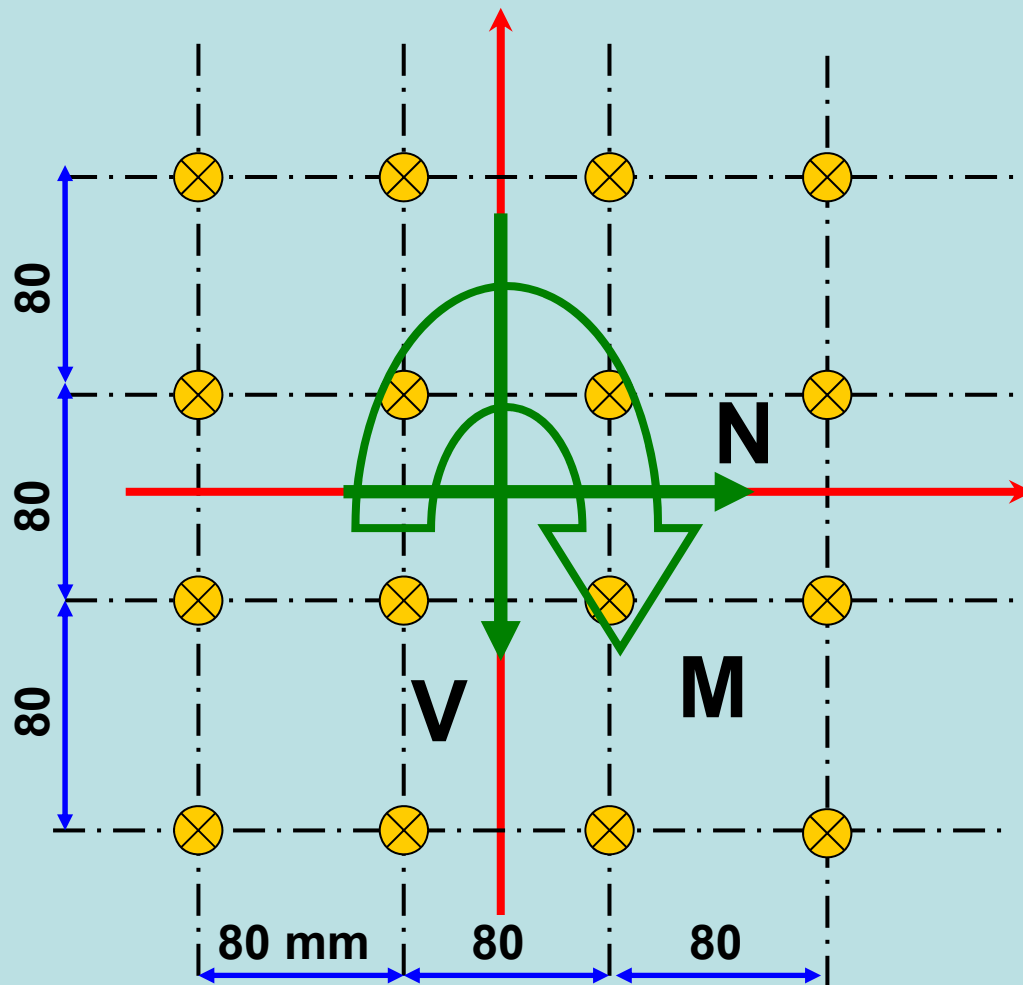
Observations concerning the geometry of the bolted connection:

- M20 bolts installed in clearance holes \Rightarrow hole diameter $d_0 = 22$ mm;
- The **horizontal end distance** between the two extreme bolt rows and the edge of the profile (or gusset plate) has been taken $e_1 = 35$ mm $= 1,59 d_0$
 $> 1,2 d_0$
- The **vertical distance** between the first and the last bolt on a row is $= 3 \times 80$ mm $= 240$ mm < 282 mm (flat zone of channel web) !

Proposed number of bolts (=16) and geometry of the connection:



The internal efforts are acting in the centre of gravity of the connection (CG):



Distribution of internal efforts on the connection bolts (V and N):

- Since the dimensions of the connection on both directions (vertical and horizontal) are equal to $240 \text{ mm} < 15d_0 = 330 \text{ mm}$, it is correct to admit an **equal distribution on the bolts for the forces V and N;**

Calculation of the design shear force per bolt produced by (N)

- Admitting an **even distribution** of (N) on all the 16 bolts of the group, we get:

$$T_N^x = \frac{N}{n_{bolts}} = \frac{60}{16} = 3,75 \text{ kN} = 375 \text{ daN}$$

- Bottom index “N” shows the provenience of the shear force per bolt (from N) and upper index “x” shows that the force vector is oriented **parallel to global axis (x-x)**.

Calculation of the design shear force per bolt produced by (V)

- Admitting an **even distribution** of (V) on all the 16 bolts of the group, we get:

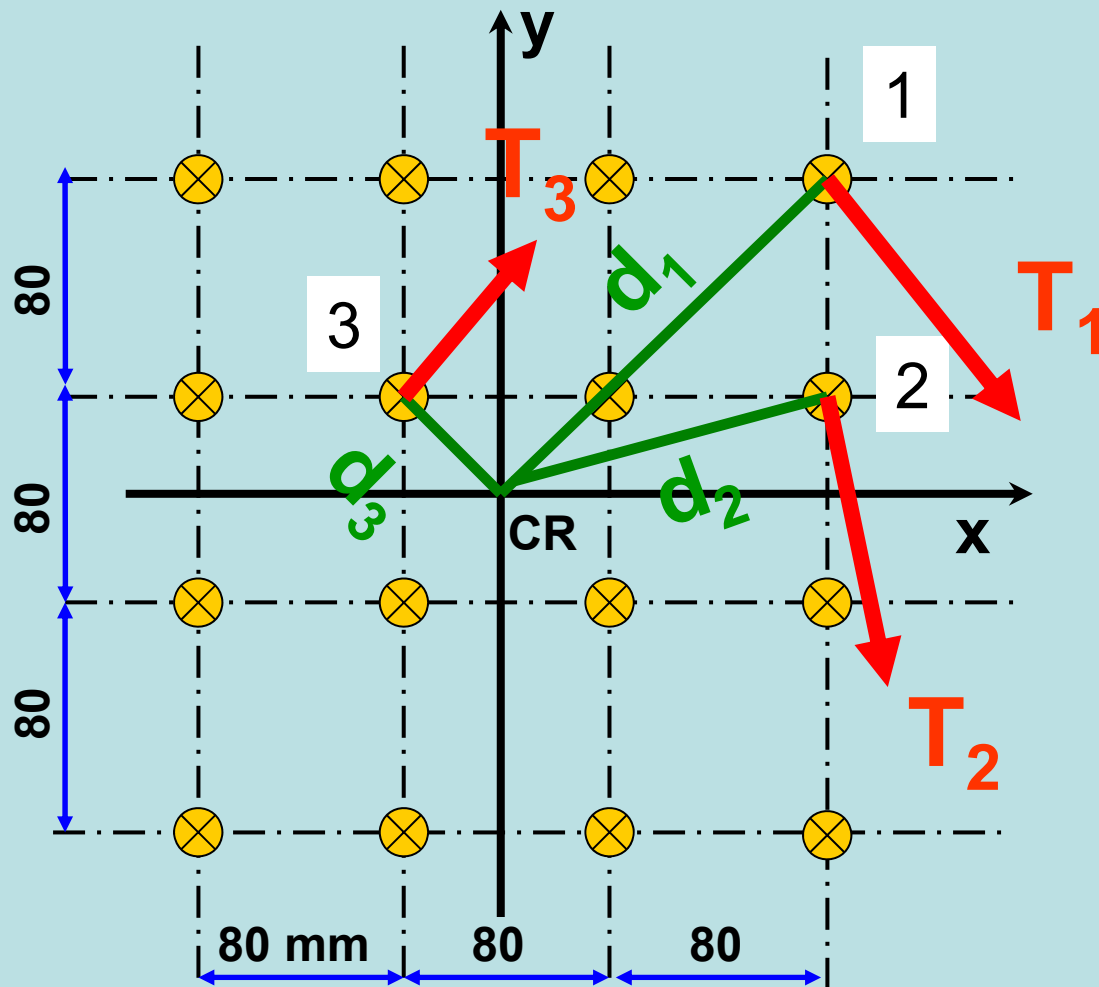
$$T_V^y = \frac{V}{n_{bolts}} = \frac{80}{16} = 5,0 \text{ kN} = 500 \text{ daN}$$

- Bottom index “V” shows the provenience of the shear force per bolt (from V) and upper index “y” shows that the force vector is oriented **parallel to global axis (y-y)**.

Distribution of internal efforts on the connection bolts (M):

- The bending moment (M) acting in the centre of rotation of the connection ($CR \equiv CG$) will be **unequally distributed on the bolts**, i.e. proportional to the distance (d_i) between each bolt (i) and point CR (see EN 1993-1-8 paragraph 3.12(1)).
- The bending moment action will produce in each point a **shear force (T_i)** perpendicular to the line representing the distance (d_i)-see next figure

Types of bolts depending on bolt distance to point $CR \equiv CG$



$$T_1 \perp d_1$$

$$T_2 \perp d_2$$

$$T_3 \perp d_3$$

From the point of view of the distance (d_i) to the centre of rotation, three types of bolts exist in the connection, i.e.:

- A number of 4 points of **type "1"** for which $x_1=12$ cm, $y_1=12$ cm (absolute values !). Distance (d_1) results
- A number of 8 points of **type "2"** for which $x_2=4$ cm, $y_2=12$ cm or $x_2=12$ cm, $y_2=4$ cm (absolute values!). Both these types lead to distance (d_2)
- A number of 4 points of **type "3"** for which $x_3=4$ cm, $y_3=4$ cm (absolute values!). Distance (d_3) results.

Using the coordinates of the three types of points (d_i) distances result:

$$\begin{cases} d_1 = \sqrt{x_1^2 + y_1^2} = \sqrt{12^2 + 12^2} = 16,97 \text{ cm} \\ d_2 = \sqrt{x_2^2 + y_2^2} = \sqrt{4^2 + 12^2} = \sqrt{12^2 + 4^2} = 12,65 \text{ cm} \\ d_3 = \sqrt{x_3^2 + y_3^2} = \sqrt{4^2 + 4^2} = 5,66 \text{ cm} \end{cases}$$

- As evident from upper results, $d_1 > d_2 > d_3$.
- According to the accepted unequal distribution of the shear forces T_i (produced by the moment M) proportional to (d_i) , we will obtain $T_1 > T_2 > T_3$
- This means that **type “1” points of the corners of the bolt group will be the most solicited**. The bolt checking procedure according to EN 1993-1-8 shall be performed in these points!

Calculation of the maximum design force per fastener (T_1) produced by the bending moment (M):

- The value of T_1 results from the following **equation of equilibrium**:

$$M = \sum_{i=1}^{16} T_i \cdot d_i$$

- The equation shows that moment (M) is equilibrated by the sum of moments of the forces (T_i) in respect to the centre of rotation CR. The sum is extended on all the 16 bolts of the group.

- Because in our particular case we have only **three types of bolts** (i.e. 1,2 and 3), the equation of equilibrium becomes:

$$M = 4 \cdot T_1 \cdot d_1 + 8 \cdot T_2 \cdot d_2 + 4 \cdot T_3 \cdot d_3$$

- At the same time, the accepted hypothesis of **uneven distribution of (T_i) forces produced by M** , proportional with the corresponding distances (d_i) has the following mathematical expression:

$$\frac{T_{1M}}{d_1} = \frac{T_{2M}}{d_2} = \frac{T_{3M}}{d_3}$$

- This gives:

$$\left\{ \begin{array}{l} \frac{T_{1M}}{d_1} = \frac{T_{2M}}{d_2} \Rightarrow T_{2M} = \frac{d_2}{d_1} \cdot T_{1M} \\ \frac{T_{1M}}{d_1} = \frac{T_{3M}}{d_3} \Rightarrow T_{3M} = \frac{d_3}{d_1} \cdot T_{1M} \end{array} \right.$$

- Thus, **all the design shear forces** produced by the moment M may be expressed in the equilibrium equation as a function of the maximum force in point (1), i.e. T_1

- The equilibrium equation between moments becomes:

$$M = 4 \cdot T_{1M} \cdot d_1 + 8 \cdot \left(\frac{d_2}{d_1} \cdot T_{1M} \right) \cdot d_2 + 4 \cdot \left(\frac{d_3}{d_1} \cdot T_{1M} \right) \cdot d_3$$

- Or, the equivalent form of the upper equation:

$$M = \frac{T_{1M}}{d_1} \cdot \left(4 \cdot d_1^2 + 8 \cdot d_2^2 + 4 \cdot d_3^2 \right)$$

- In this last equation, only T_{1M} is unknown: all other elements are known data of the problems

- The formula to calculate the maximum design shear force produced by the bending moment (M) becomes:

$$T_{1M} = \frac{M \cdot d_1}{4 \cdot d_1^2 + 8 \cdot d_2^2 + 4 \cdot d_3^2} = M \cdot \frac{d_1}{\sum_1^{n.bolts} d_i^2}$$

- Observation: The shear force vector is **NOT parallel to the global axes (x-x) or (y-y)**. By the admitted design hypothesis, the vector has its origin in point (1) and is **perpendicular** to the line drawn through points CR and (1).

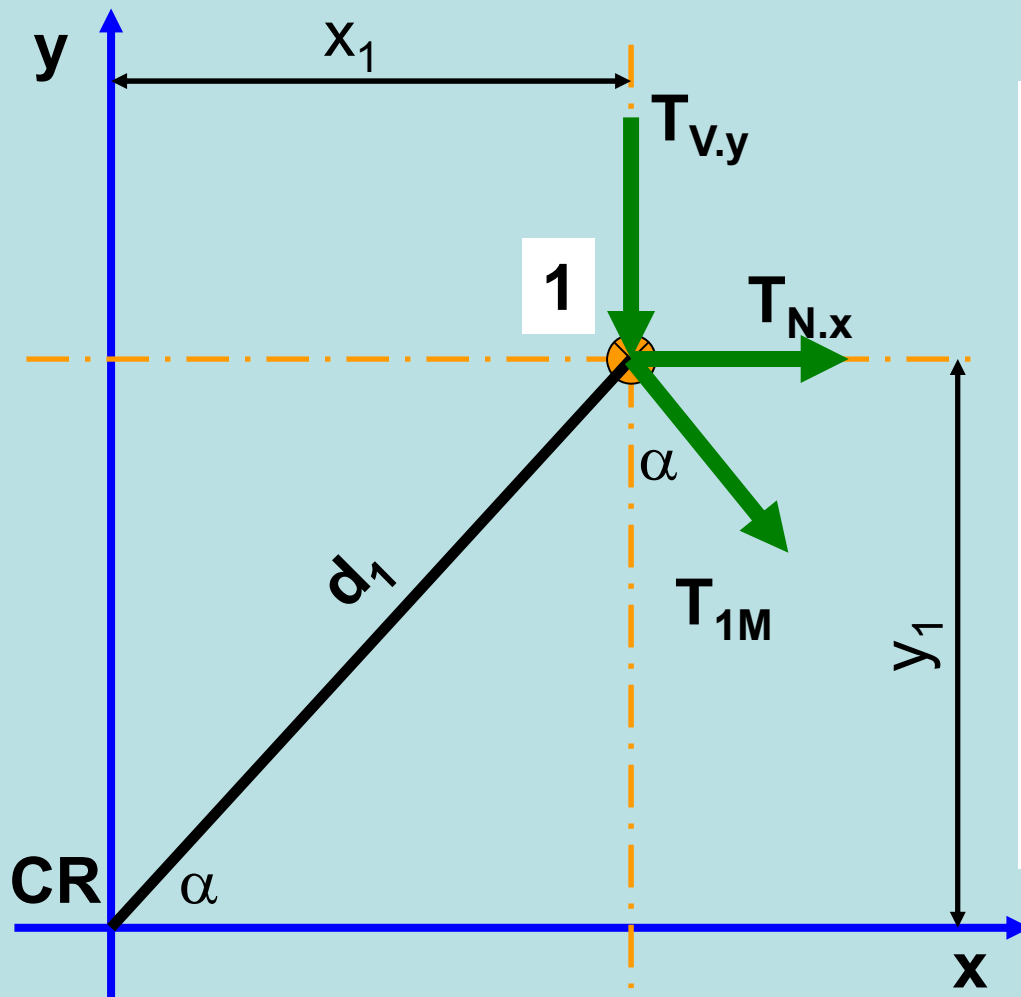
Using (M) value and previously calculated values of distances d_1 , d_2 , d_3 we get:

$$M = 96 \text{ kNm} = 960000 \text{ daNcm}$$

$$T_{1M} = \frac{960000 \cdot 16,97}{4 \cdot 16,97^2 + 8 \cdot 12,65^2 + 4 \cdot 5,66^2} = 6366 \text{ daN}$$

This is the **maximum design shear force** produced by moment M and acting **on the most solicited bolt from the group**, i.e. bolt type 1 located in the corner.

In point (1) are simultaneously acting the design shear forces produced by N, V and M:



The resultant design shear force in point 1 (the most solicited bolt of the group) is the **vectorial sum between $T_{V.y}$, $T_{N.x}$ and T_{1M} vectors**

In order to obtain this sum we need to calculate the **projections of vector T_{1M} on the (x-x) and (y-y) axes** (i.e. $T_{1M.x}$ and $T_{1M.y}$)

Calculation of T_{1M} projections using vector angle (α) to global axes:

$$tg \alpha = \frac{y_1}{x_1} \Rightarrow \alpha = arctg\left(\frac{y_1}{x_1}\right) = arctg\left(\frac{12,0}{12,0}\right) = 45^0$$

$$\begin{cases} T_{1M}^x = T_{1M} \cdot \sin 45^0 = 6363 \cdot \sin 45^0 = 4499 \text{ daN} \\ T_{1M}^y = T_{1M} \cdot \cos 45^0 = 6363 \cdot \cos 45^0 = 4499 \text{ daN} \end{cases}$$

Observation: we are here in the **fortunate case** when $\alpha=45^0$!
In practice (α) angle may take any value, depending on the proposed geometry for the connection!

Second method to calculate the projections on the global axes for T_{1M} vector :

- By observing that, for every point (i) in the bolt group we have the relation:

$$d_i^2 = x_i^2 + y_i^2$$

- the **projections of vector T_{1M}** on the global axes may be obtained using a similar procedure as before:

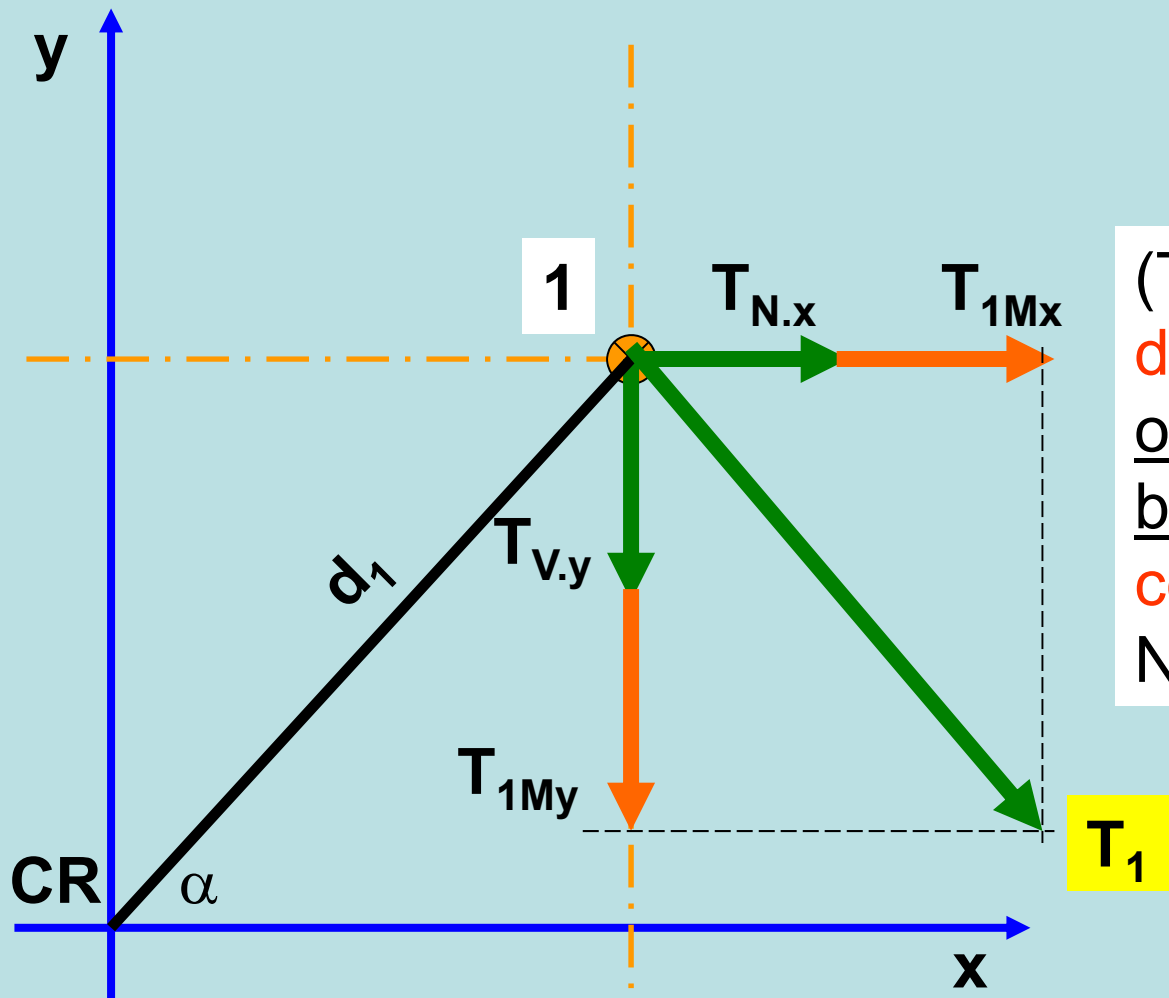
$$\begin{cases} T_{1M}^x = M \cdot \frac{y_1}{\sum_i (x_i^2 + y_i^2)} \\ T_{1M}^y = M \cdot \frac{x_1}{\sum_i (x_i^2 + y_i^2)} \end{cases}$$

Observation: Last formulae obtained are in fact an **easier way** to calculate T_{1M} components on the global axes, since (x_i) and (y_i) coordinates are **known from the beginning** from the proposed geometry of the bolt group

$$\left\{ \begin{array}{l} T_{1M}^x = 960000 \cdot \frac{12}{4 \cdot (12^2 + 12^2) + 8 \cdot (4^2 + 12^2) + 4 \cdot (4^2 + 4^2)} = 4500 \text{ daN} \\ T_{1M}^y = 960000 \cdot \frac{12}{4 \cdot (12^2 + 12^2) + 8 \cdot (4^2 + 12^2) + 4 \cdot (4^2 + 4^2)} = 4500 \text{ daN} \end{array} \right.$$

The result is identical to the first method, but obtained on an easier way!

Superposition of the effects of N, V and bending moment M in point (1) is done by using the vector projections on global axes:



(T_1) is the **resulting design shear force** on the most solicited bolt of the group from **combined effect** of N, V and M

Calculation of the resulting T_1 value as a
sum of vector projections:

$$T_1 = \sqrt{\left(T_N^x + T_{1M}^x\right)^2 + \left(T_V^y + T_{1M}^y\right)^2}$$

Using previously calculated values, this gives:

$$T_1 = \sqrt{(375 + 4500)^2 + (500 + 4500)^2} = 6983 \text{ daN}$$

This final value shall be compared to bolt resistances according to EN 1993-1-8.

Checking relations according to EN 1993-1-8, Table 3.2:

- For bolted connections of category A – bearing type, the following relations are prescribed for checking:

$$\begin{cases} F_{v,Ed} \leq F_{v,Rd} \\ F_{v,Ed} \leq F_{b,Rd} \end{cases}$$

- In which $F_{v,Ed} = T_1 =$ design shear force acting on the most solicited bolt (i.e. bolt type 1)

In previous checking relations:

- $F_{v,Rd}$ = **shear resistance of the bolt per shear plane**: if several shear planes exist (as in present case, where we have $n_{sh} = 2$ shear planes) the resulting shear resistance per plane shall be multiplied with (n_{sh});
- $F_{b,Rd}$ = **bearing resistance of the minimum thickness plate package** connected by the bolt (in our case, the gusset plate which thickness is $< 2 \times$ channel web thickness)

Calculation of the bolt shear resistance:

- The shear resistance of the bolt per shear plane according to Table 3.4:

$$F_{v,Rd} = \frac{\alpha_v \cdot f_{ub} \cdot A}{\gamma_{M2}}$$

- In the present case, the bolt is intersecting two shear planes, so its shear resistance becomes:

$$F_{v,Rd} = 2 \cdot \frac{\alpha_v \cdot f_{ub} \cdot A}{\gamma_{M2}}$$

In the shear resistance formula:

- $\alpha_v = 0,6$ (for the studied case, where the **shear planes intersect the non-threaded part** of the bolt shank: this is usual for normal bolts of grades 4.6 of 5.6 or 6.6)
- A =gross area of the bolt cross-section

$$A = \frac{\pi \cdot d^2}{4} = \frac{\pi \cdot 2^2}{4} = 3,14 \text{ cm}^2$$

- $f_{ub} = 5 \times 10 = 50 \text{ daN/mm}^2 = 5000 \text{ dan/cm}^2$ for gr.5.6 bolts

Calculation of the bolt shear resistance:

- For the two shear planes:

$$F_{v,Rd} = 2 \cdot \frac{0,6 \cdot 5000 \cdot 3,14}{1,25} = 15.072 \text{ daN} > F_{v,Ed} = 6983 \text{ daN}$$

First checking to Table 3.2 OK!

Calculation of the bearing resistance

- Under shear force action, the gusset plate tends to move in one direction, while the two channel sections connected by the bolt group tend to move in opposite direction.
- **Gusset thickness** $t = 15 \text{ mm}$ (steel S275 !)
- The **sum of web thickness** for the channel section $= 2 \cdot t_w = 2 \cdot 14 \text{ mm} = 28 \text{ mm} > t$
- So, the **minimum thickness package is the gusset plate** (to check for bearing!).

Calculation of the bearing resistance for the gusset plate:

- The bearing resistance shall be calculated according to Table 3.4:

$$F_{b,Rd} = \frac{k_1 \cdot \alpha_b \cdot f_u \cdot d \cdot t}{\gamma_{M2}}$$

- In which:
 - f_u = ultimate strength of gusset steel (S275) = 4400 daN/cm²
 - d = bolt nominal diameter = 20 mm = 2,0 cm
 - t = gusset thickness = 15 mm = 1,5 cm

Calculation of the k_1 value in the bearing formula:

- d_0 = clearance hole diameter = 22 mm = 2,2 cm

$$k_1 = \min \left\{ 2,8 \cdot \frac{e_2}{d_0} - 1,7; 2,5 \right\}$$

- and:

$$2,8 \cdot \frac{e_2}{d_0} - 1,7 = 2,8 \cdot \frac{35}{22} - 1,7 = 2,75$$

$$\Rightarrow k_1 = \min \{ 2,75; 2,5 \} = 2,5$$

Calculation of the (α_b) value in the bearing formula:

$$\alpha_b = \min \left\{ \alpha_d ; \frac{f_{ub}}{f_u} ; 1,0 \right\}$$

where:

$$\left\{ \begin{array}{l} \alpha_d = \frac{e_1}{3 \cdot d} = \frac{35}{3 \cdot 22} = 0,53 \\ \frac{f_{ub}}{f_u} = \frac{5000}{4400} = 1,136 \end{array} \right.$$

$$\Rightarrow \alpha_b = \min \{ 0,53 ; 1,135 ; 1,0 \} = 0,53$$

Calculation of the bearing resistance and checking:

$$F_{b,Rd} = \frac{2,5 \cdot 0,53 \cdot 4400 \cdot 2,0 \cdot 1,5}{1,25} = 13992 \text{ daN} > F_{v,Ed} = 6983 \text{ daN}$$

Second checking to Table 3.2 OK!

Comment on the result: the design shear force value is approximately 50% of the minimum resistance which suggests **a group of bolts excessively strong**. Normally, the number of bolts should be diminished (for example 3 bolts instead of 4 on each vertical row) and **the whole procedure repeated** to obtain a more rational result.

PART 4:

Shear connection under shear force
and bending moment. Version 2:

Category C shear connection –slip
resistant at ultimate limit state

Initial data:

- The same cantilever beam as in Part 3 example is used, of identical materials;
- Loading is identical;
- The same proposed group of bolts is used for the shear connection, except for the type of bolts: **M20 gr.10.9 preloaded**
- The bolted connection will be treated as a **shear connection of category C: slip resistant at ultimate limit state**

Design shear force acting on the most solicited bolt:

- The **design shear force** acting on the most solicited bolt (type 1 in the corner of the bolt group) will be the same as before:

$$T_1 = F_{v,Ed} = 6983 \text{ daN}$$

The same hypothesis for **N, V and M distributions** have been applied in this case, leading to the same design shear force value.

Checking relations for the slip resistant connection according to Table 3.2:

$$\begin{cases} F_{v,Ed} \leq F_{s,Rd} \\ F_{v,Ed} \leq F_{b,Rd} \\ F_{v,Ed} \leq N_{net,Rd} \end{cases}$$

Resistance values in checking relations:

- $F_{s,Rd}$ = **design slip resistance** of the preloaded bolt
- $F_{b,Rd}$ = **bearing resistance** of the gusset plate (as before) at ultimate limit state when the preloaded bolts loosen and friction disappears;
- $N_{net,Rd}$ = **resistance of gusset to tension in the net area**: this checking makes no sense here because of the **non-uniform distribution** of the design shear force on the bolt group.

Calculation of the design slip resistance per bolt:

According to paragraph 3.9.1(1) of EN1993-1-8, the design slip resistance formula for a preloaded bolt is:

$$\begin{cases} F_{s,Rd} = \frac{k_s \cdot n \cdot \mu}{\gamma_{M3}} \cdot F_{p,C} \\ F_{p,C} = 0,7 \cdot f_{ub} \cdot A_s \end{cases}$$

in which $F_{p,C}$ is the design preloading force of the bolt - see paragraph 3.9.1(2).

Explanation of terms in $F_{p,C}$ formula:

- Employed bolts: M20 gr.10.9
- Resulting data (from bolt grade symbol):
 - $f_{ub} = 10 \times 10 = 100 \text{ daN/mm}^2 = 10000 \text{ daN/cm}^2$
 - Nominal diameter of the bolt: $d = 20 \text{ mm} = 2 \text{ cm}$
 - Resistant diameter: $d_{res} = 0,89 \cdot d = 1,78 \text{ cm}$

$$\Rightarrow A_s = \frac{\pi \cdot d_{res}^2}{4} = \frac{\pi \cdot 1,78^2}{4} = 2,487 \text{ cm}^2$$

Calculation of the design preloading force:

- The value of the design preloading force results:

$$F_{p,C} = 0,7 \cdot 10000 \cdot 2,487 = 17.409 \text{ daN}$$

- This is the value of the **tension forced induced into the bolt shank** by the preloading operation of the bolt (tightening).

Value of coefficients k_s, n, μ

- $k_s = 1,0$ (holes with standard nominal clearance - from Table 3.6)
- $n = 2$ (number of friction surfaces, i.e. one gusset plate between two back to back channel sections)
- $\mu = 0,3$ (slip factor for class C surface according to Table 3.7)

Calculation of the design slip resistance and checking:

$$F_{s,Rd} = \frac{1,0 \cdot 2 \cdot 0,3}{1,25} \cdot 17409 = 8356 \text{ daN} > F_{v,Ed} = 6983 \text{ daN}$$

First checking to Table 3.2 OK!

Comment on the obtained result: The slip resistance value is **reasonably close to the design shear force**, which indicates a rational proposal for the group of bolts, working as a slip resistant connection. **No change of bolt geometry or other connection component is required in this case!**

Calculation of the bearing resistance for the gusset plate :

- The bearing resistance shall be calculated according to Table 3.4 for a bolt with **entirely threaded shank**, (as high strengths bolts of gr.10.9 usually are!)
- (ultimate limit state when preloaded bolts loosen and slip occurs) :

$$F_{b,Rd} = \frac{k_1 \cdot \alpha_b \cdot f_u \cdot d_{res} \cdot t}{\gamma_{M2}}$$

Calculation of the coefficients in bearing resistance formula:

- In the previous formula:
 - f_u = ultimate strength of gusset steel (S275)
= 4400 daN/cm²
 - d_{res} = bolt resistant diameter = $0,89 \cdot 20$ mm
= 1,78 cm
 - t = gusset thickness = 15 mm = 1,5 cm

Calculation of the k_1 value in the bearing formula:

- d_0 = clearance hole diameter = 22 mm = 2,2 cm

$$k_1 = \min \left\{ 2,8 \cdot \frac{e_2}{d_0} - 1,7; 2,5 \right\}$$

- and:

$$2,8 \cdot \frac{e_2}{d_0} - 1,7 = 2,8 \cdot \frac{35}{22} - 1,7 = 2,75$$

$$\Rightarrow k_1 = \min \{ 2,75; 2,5 \} = 2,5$$

Calculation of the (α_b) value in the bearing formula:

$$\alpha_b = \min \left\{ \alpha_d ; \frac{f_{ub}}{f_u} ; 1,0 \right\}$$

where:

$$\left\{ \begin{array}{l} \alpha_d = \frac{e_1}{3 \cdot d} = \frac{35}{3 \cdot 22} = 0,53 \\ \frac{f_{ub}}{f_u} = \frac{5000}{4400} = 1,136 \end{array} \right.$$

$$\Rightarrow \alpha_b = \min \{ 0,53 ; 1,135 ; 1,0 \} = 0,53$$

Calculation of the gusset bearing resistance and checking:

$$F_{b,Rd} = \frac{2,5 \cdot 0,53 \cdot 4400 \cdot 1,78 \cdot 1,5}{1,25} = 12452 \text{ daN} > F_{v,Ed} = 6983 \text{ daN}$$

Second checking to Table 3.2 OK!

The third checking required in Table 3.2 of the code (resistance in the net area of the gusset plate) is **NOT required** in this case because of the **un-equal distribution of the design shear force over the bolt group**.

Consequently, this second checking concludes the procedure for the slip resistant connection.