

# ANALYSIS OF PRECIPITATION SERIES AND DOUBLE MASS CURVE

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**Abstract:** The examination of precipitation series and the application of the double mass curve constitute pivotal components in the fields of hydrology and climatology. This research paper endeavors to ascertain the double mass curve, validate the consistency of the scrutinized data series, and subsequently utilize the double mass curve to rectify the discrepancies in the precipitation data. Such inconsistencies may arise from alterations in data collection methodologies or from physical changes that influence the underlying relationships. Upon the adjustment and homogenization of the data, we advance to the substantive statistical analysis, which employs the Simple Mass Curve as a visual trend tool, while fundamentally relying on frequency methods for the computation of design values.

**Keywords:** precipitation, double mass curve, temperature, catchment area

## 1. INTRODUCTION

Precipitation monitoring is very important for the efficient management of water resources, flood forecasting, etc., and precipitation of the countries is the main source of water for the hydrological system [1]. The coverage and accuracy of existing instruments are inherently limited, and achieving extensive coverage with rain gauges incurs substantial costs. Although advancements in satellite meteorological products, from TRMM to GPM, have significantly enhanced both coverage and spatial-temporal resolution, measurement errors and sampling uncertainties continue to constrain their applicability [2].

The objectives of this study were to analyze the long-term rain gauge records from 1991 to 2020 at two stations, Deva and Lugoj, situated at the extremities of the Bistra River basin, and to assess the homogeneity of the rain gauge data series between these two stations. This element is vital to ensure that the discrepancies identified in the data are ascribed to genuine climatic variations rather than external influences.

## 2. THE CASE STUDY

The Bistra River originates in the Țarcu Mountains, with a length of 46.2 km and a catchment area of 908 km<sup>2</sup>. From an ecological, economic and hydrological point of view, the river network of Bistra catchment area is very important. It plays an essential role in the local ecosystem through the water resources offered, and from a tourist point of view, Bistra River offers a multitude of landscapes and recreational areas.

The main tributary of the Bistra River is the Rusca River, which originates from the Padeș Peak at 1359

meters altitude and has an area of 160 km<sup>2</sup> and a length of 21 km.

Altitude plays an important role in the distribution of temperature and precipitation (the higher the altitude, the lower the temperature and, usually, the greater the precipitation).

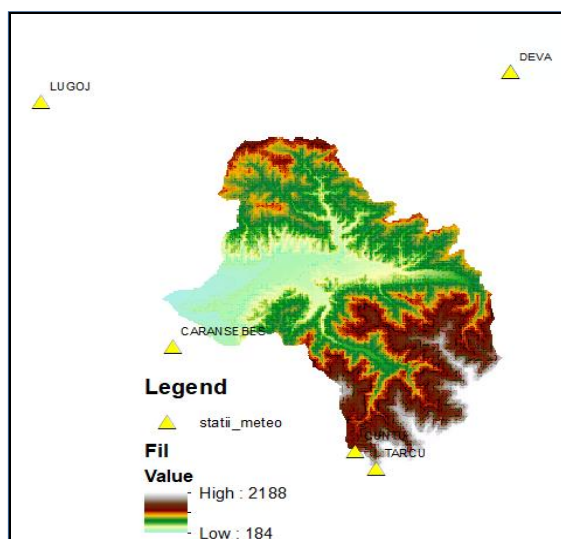


Figure1. Location map of the study area

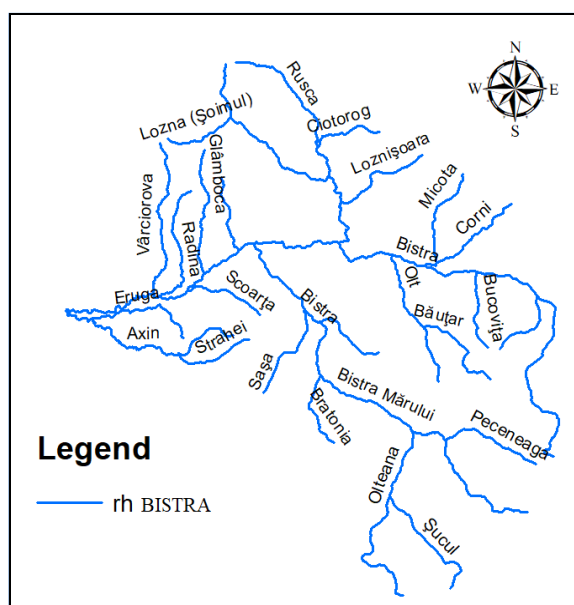
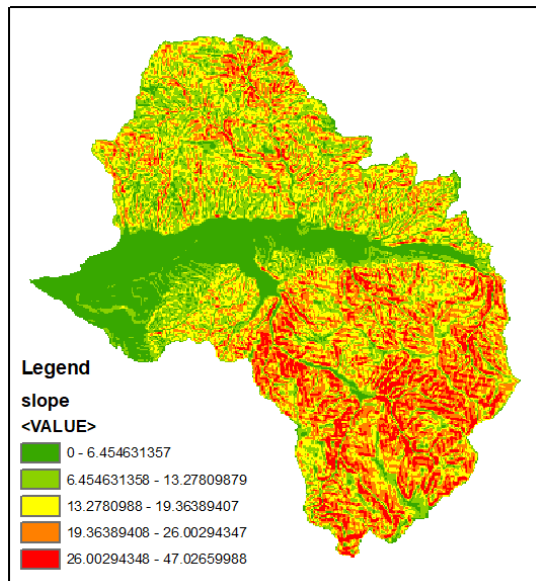


Figure 2. The hydrographical network of River Bistra

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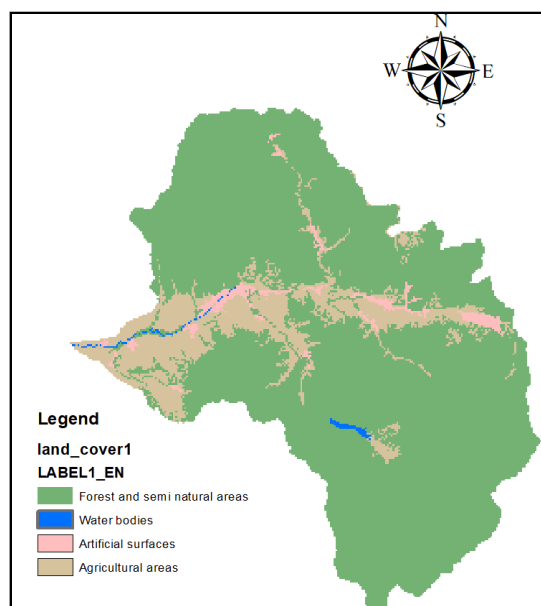
The basin surfaces have an average slope with very high values, between 300 and 400 m/km. The water course has high falls in its mountainous sector, reaching an average of 80 m/km before reaching the town of Bucova.



**Figure 3.** The slope of Bistra catchment

In the spring area, the slope exceeds 10-15%, in the hilly area with values between 5-10%, and in the lower area, close to the outlet, it has values below 5%. The terrain of the Bistra River Basin is predominantly formed by forests and semi-natural areas, the water bodies, artificial surfaces and agricultural areas (figure 4).

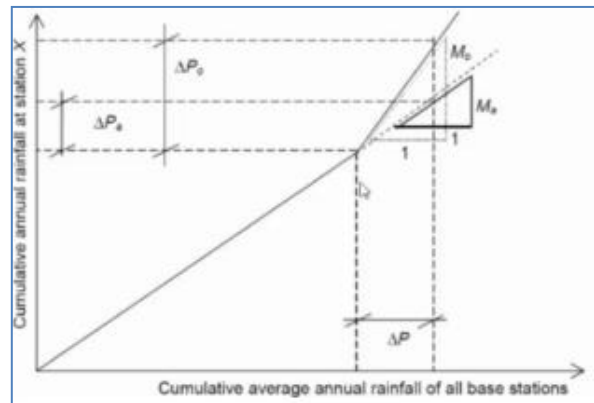
The climate encountered in the Bistra River Basin is temperate continental, manifested by hot summers and cold winters.



**Figure 4.** The land cover of River Bistra

### 3. RESULTS AND CONCLUSIONS.

Essentially, the analysis of precipitation series begins with checking the homogeneity using the Double Mass Curve to validate the quality of the data [3]. The mass curve is used to detect the influence of anthropogenic factors and climate change in the data series used for hydrological modeling. If the mass curve is not characterized by "jumps", then the flow formation process in the studied area is homogeneous and vice versa.[8]



**Figure 5.** The double mass curve

$$P_a = P_o \frac{M_a}{M_o}$$

Where:

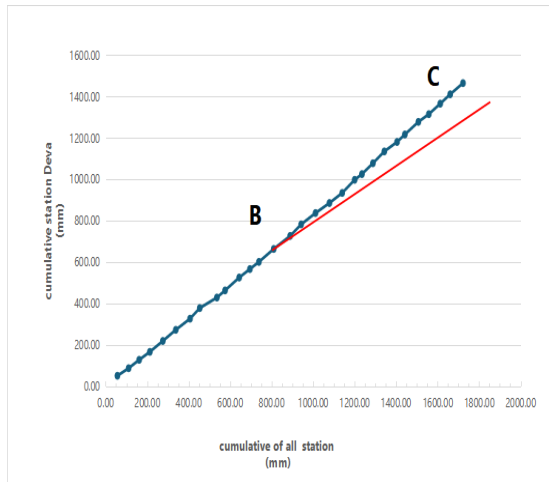
Mo - Slope of the line before the breakpoint.

Ma - Slope of the line after the breakpoint

Figure 5 shows the relationship between the rainfall measured at a station (station X) and the average rainfall of the reference stations.

The consistency check consists of an unchanged (consistent) relationship which is represented by a straight line. Any slope break (change in the angle of the line) indicates a change in the data collection regime at Station X; these changes can be caused by moving the station, changing the measuring instruments, changes in the station's environment (e.g. deforestation, high-rise buildings). Next, by applying a correction factor, the data prior to the slope break is adjusted to the current conditions (or vice versa), so that the data series becomes homogeneous (consistent).

By adjusting the inconsistent series, double mass curve ensures that subsequent hydrological and climatic analyses (such as the calculation of the average rainfall per basin or frequency analysis) are based on correct and homogeneous data.

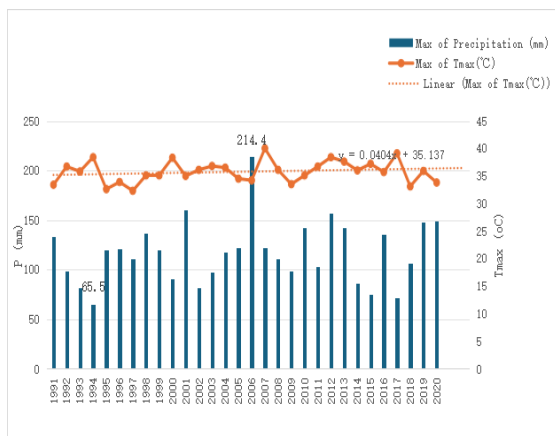


**Figure 5.** The double mass curve of Deva station

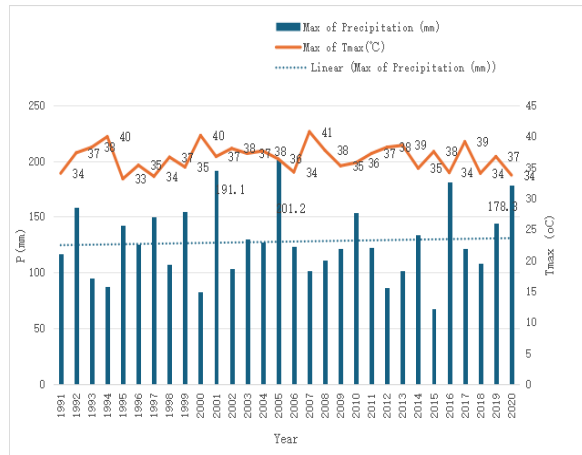
Point B on the data curve is the slope break point. Here, the behavior of the Deva station has changed in relation to the regional average. The segment from Point B to Point C regarding the correct slope of the series reflects the consistent regime of the Deva station after the change. The goal is to adjust the values recorded in the original period to make them correspond to the correct slope stability regime.

In the graphs below, the trends of the average annual precipitation, respectively of the maximum temperatures recorded, have been analyzed. As can be seen in figure 1, the highest amount of precipitation was recorded in 2006, and in 1994 only 65.5 mm was recorded at Deva station. Regarding the maximum temperatures, a linear trend with a slight increase can be observed.

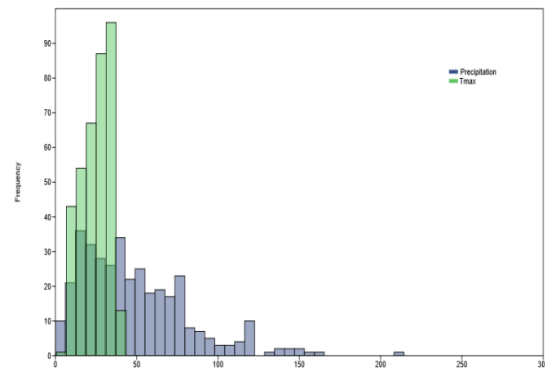
The figure 7 shows that the frequencies decrease rapidly as the interval size increases, indicating a strong positive asymmetry specific to the precipitation data; in the case of maximum temperatures, the distribution appears to be roughly centered in the range of approximately 25 - 37, approximating a normal temperature distribution.



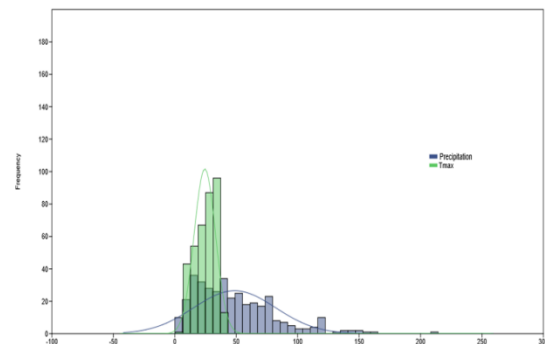
**Figure 6.** The yearly maximum precipitation and temperature of Deva station



**Figure 7.** The yearly maximum precipitation and temperature of Lugoj station



**Figure 8.** The frequency of precipitation and temperature from Deva station



**Figure 9.** Fit normal – Distribution of numerical data (histogram)

**Table 1.** Distribution of precipitation and maximum temperatures from Deva station

 Histogram

| Histogram | Numbers |               |           |           |      |           |           |
|-----------|---------|---------------|-----------|-----------|------|-----------|-----------|
| Bin start | Bin end | Precipitation | 95% CI lo | 95% CI hi | Tmax | 95% CI lo | 95% CI hi |
| 0         | 6.1257  | 10            | 4.8236    | 18.177    | 1    | 0.025317  | 5.5365    |
| 6.1257    | 12.251  | 21            | 13.128    | 31.605    | 43   | 31.609    | 56.705    |
| 12.251    | 18.377  | 36            | 25.568    | 48.873    | 54   | 41.303    | 68.816    |
| 18.377    | 24.503  | 32            | 22.173    | 44.342    | 67   | 53.005    | 82.889    |
| 24.503    | 30.629  | 28            | 18.828    | 39.764    | 87   | 71.397    | 104.16    |
| 30.629    | 36.754  | 26            | 17.178    | 37.454    | 96   | 79.799    | 113.6     |
| 36.754    | 42.88   | 34            | 23.865    | 46.613    | 13   | 6.9713    | 21.946    |
| 42.88     | 49.006  | 22            | 13.928    | 32.784    | 0    | 0         | 3.6701    |
| 49.006    | 55.131  | 25            | 16.359    | 36.293    | 0    | 0         | 3.6701    |
| 55.131    | 61.257  | 18            | 10.763    | 28.035    | 0    | 0         | 3.6701    |
| 61.257    | 67.383  | 19            | 11.545    | 29.231    | 0    | 0         | 3.6701    |
| 67.383    | 73.509  | 17            | 9.9883    | 26.833    | 0    | 0         | 3.6701    |
| 73.509    | 79.634  | 23            | 14.734    | 33.959    | 0    | 0         | 3.6701    |
| 79.634    | 85.76   | 8             | 3.471     | 15.594    | 0    | 0         | 3.6701    |
| 85.76     | 91.886  | 7             | 2.8269    | 14.275    | 0    | 0         | 3.6701    |
| 91.886    | 98.011  | 5             | 1.6289    | 11.561    | 0    | 0         | 3.6701    |
| 98.011    | 104.14  | 3             | 0.61986   | 8.6975    | 0    | 0         | 3.6701    |
| 104.14    | 110.26  | 3             | 0.61986   | 8.6975    | 0    | 0         | 3.6701    |
| 110.26    | 116.39  | 4             | 1.0928    | 10.153    | 0    | 0         | 3.6701    |
| 116.39    | 122.51  | 10            | 4.8236    | 18.177    | 0    | 0         | 3.6701    |
| 122.51    | 128.64  | 0             | 0         | 3.6701    | 0    | 0         | 3.6701    |
| 128.64    | 134.77  | 1             | 0.025317  | 5.5365    | 0    | 0         | 3.6701    |
| 134.77    | 140.89  | 2             | 0.24246   | 7.1726    | 0    | 0         | 3.6701    |
| 140.89    | 147.02  | 2             | 0.24246   | 7.1726    | 0    | 0         | 3.6701    |
| 147.02    | 153.14  | 2             | 0.24246   | 7.1726    | 0    | 0         | 3.6701    |
| 153.14    | 159.27  | 1             | 0.025317  | 5.5365    | 0    | 0         | 3.6701    |
| 159.27    | 165.39  | 1             | 0.025317  | 5.5365    | 0    | 0         | 3.6701    |
| 165.39    | 171.52  | 0             | 0         | 3.6701    | 0    | 0         | 3.6701    |
| 171.52    | 177.65  | 0             | 0         | 3.6701    | 0    | 0         | 3.6701    |
| 177.65    | 183.77  | 0             | 0         | 3.6701    | 0    | 0         | 3.6701    |
| 183.77    | 189.9   | 0             | 0         | 3.6701    | 0    | 0         | 3.6701    |
| 189.9     | 196.02  | 0             | 0         | 3.6701    | 0    | 0         | 3.6701    |
| 196.02    | 202.15  | 0             | 0         | 3.6701    | 0    | 0         | 3.6701    |
| 202.15    | 208.27  | 0             | 0         | 3.6701    | 0    | 0         | 3.6701    |
| 208.27    | 214.4   | 1             | 0.025317  | 5.5365    | 0    | 0         | 3.6701    |

Table 1 shows the distribution of precipitation and maximum temperatures ( $T_{\max}$ ) from a Deva station, after the corrections established using the double mass curve were applied. The precipitation column shows the frequency (number of occurrences) of the values in the respective class, and the 95% CI lo (lower limit) and 95% CI hi (upper limit) columns show the intervals in which the true population mean is expected to fall, with a probability of 95%.

This analysis is important in hydrology, because it is then used to build a statistical model of the precipitation regime. Ensuring that the collected precipitation data is homogeneous and their statistical adjustment was done using the correction factor. Based on the resulting (homogenized) data series, statistical analysis was performed, being divided into classes (bins) to build Frequency Histograms (Figure 8 and 9) that show the distribution of the variables.

These distributional analyses are essential for hydrological modeling, allowing for the estimation of risks (e.g. frequency of floods or droughts) based on probabilities.

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